

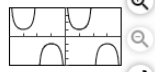
Use properties of natural logarithms and fundamental trigonometric identities to show that the pair of expressions is equivalent.

$$\ln |\tan x| + \ln |\cos x| \text{ and } \ln |\sin x|$$

*on Board*

In the following exercise, half of an identity and the graph of this half are given. Use the graph to make a conjecture as to what the right side of the identity should be. Then prove your conjecture.

$$\frac{(\csc x + \cot x)(\csc x - \cot x)}{\sin x} = ?$$

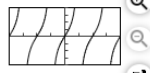


$[-2\pi, 2\pi, \pi/2]$  by  $[-4, 4, 1]$

*on Board*

In the following exercise, half of an identity and the graph of this half are given. Use the graph to make a conjecture as to what the right side of the identity should be. Then prove your conjecture.

$$\frac{1}{\sec x - \tan x} - \frac{1}{\sec x + \tan x} = ?$$



$[-2\pi, 2\pi, \pi/2]$  by  $[-4, 4, 1]$

*on Board*

Verify the identity. 
$$\frac{\cos x - \sin x - 1}{\cos x + \sin x + 1} = \frac{\cos x - 1}{\sin x}$$

*on Board*

Verify the identity.

$$\csc t \cot t = \frac{1 + \cot^2 t}{\sec t}$$

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Verify the identity.

$$\frac{\sin \theta + \cos \theta}{\sin \theta} + \frac{\cos \theta + \sin \theta}{\cos \theta} = 2 + \sec \theta \csc \theta$$

Use properties of natural logarithms and fundamental trigonometric identities to show that the pair of expressions is equivalent.

$$\ln |1 + \cos \theta| - 2 \ln |\sin \theta| \text{ and } -\ln |1 - \cos \theta|$$

Verify the identity.

$$\frac{\csc(2\theta) - \sin(2\theta)}{\cos(2\theta)} = \cot(2\theta)$$

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Verify the identity.

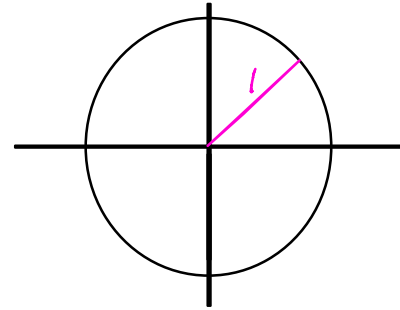
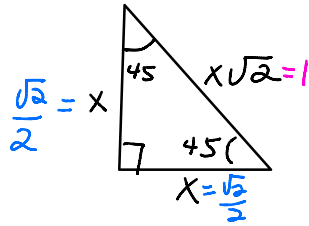
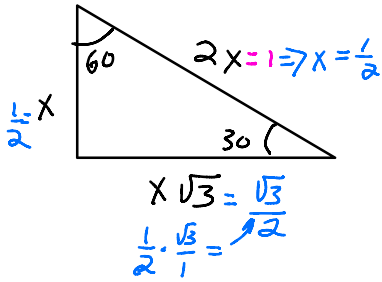
$$\sec^2 x \csc^2 x = \sec^2 x + \csc^2 x$$

Verify the identity.

$$\frac{\csc \theta \sin \theta}{\cot \theta} = \tan \theta$$

unit circle

radius = 1



$\frac{x\sqrt{2}}{\frac{\sqrt{2}}{2}} = \frac{1}{\frac{\sqrt{2}}{2}}$   
 $x = \frac{\sqrt{2}}{2}$

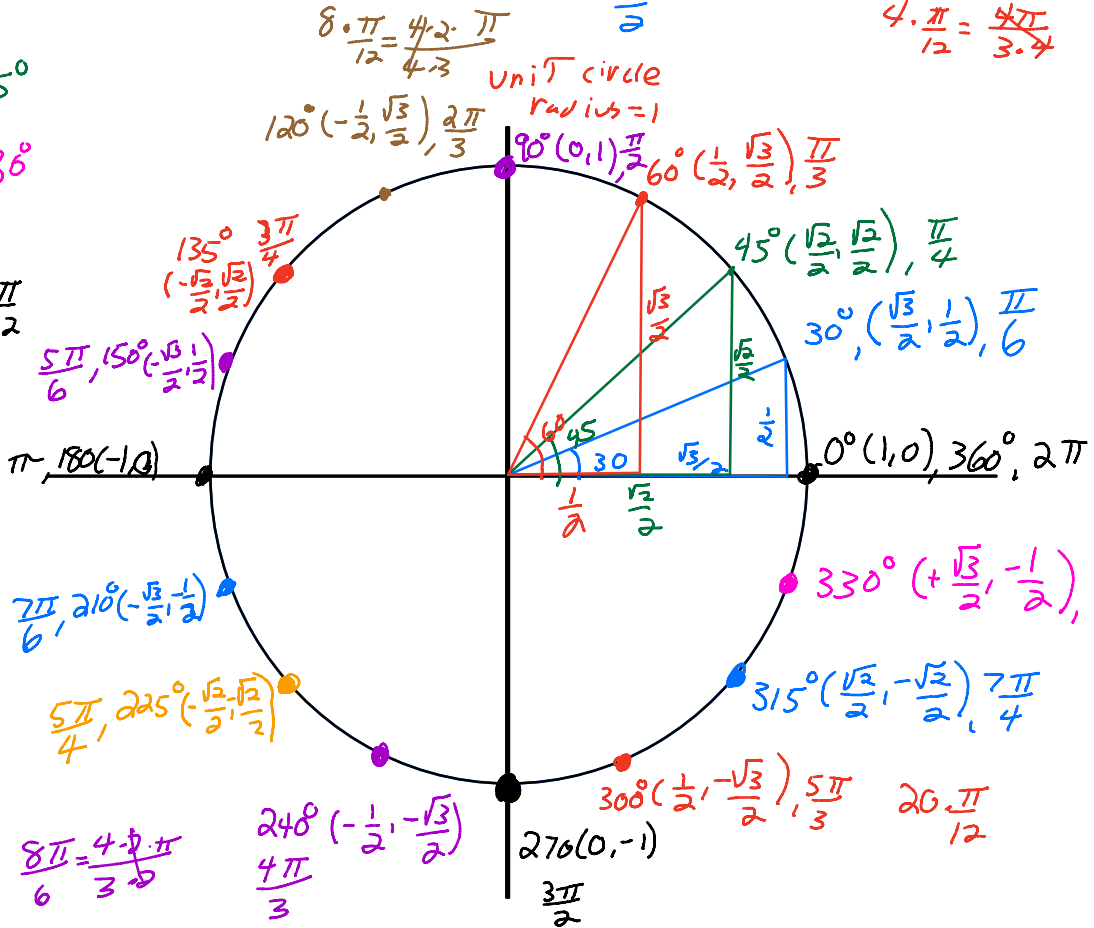
$\frac{4 \cdot \pi}{12} = \frac{\pi}{3}$

$\frac{\pi}{12} \approx 15^\circ$

$\frac{2 \cdot \pi}{12} = \frac{\pi}{6} \approx 30^\circ$

$\frac{150^\circ}{12} \approx 10 \cdot \frac{\pi}{12}$

$\frac{150^\circ}{6} \approx \frac{5\pi}{6}$



$\frac{8 \cdot \pi}{12} = \frac{4 \cdot 2 \cdot \pi}{4 \cdot 3}$

Unit circle radius = 1

$\frac{14 \cdot \pi}{12}$

$\frac{2\pi}{6}, 210^\circ (-\frac{\sqrt{3}}{2}, -\frac{1}{2})$

$\frac{5\pi}{4}, 225^\circ (-\frac{\sqrt{2}}{2}, -\frac{\sqrt{2}}{2})$

$\frac{8\pi}{6} = \frac{4 \cdot 2 \cdot \pi}{3 \cdot 2}$

$\frac{4\pi}{3}, 240^\circ (-\frac{1}{2}, -\frac{\sqrt{3}}{2})$

$\frac{3\pi}{2}, 270^\circ (0, -1)$

$\frac{20 \cdot \pi}{12}$